2 Preliminaries

Reinforcement learning stems from a kind of "trial and error" approach. For instance, in the process of game training, when Agent wins, the trainer gives Agent a positive reward, when Agent fails, the trainer gives negative incentive, and otherwise the result is zero. Thus, Agent could learn to select a series of actions in order to get the highest reward from the indirect tardy rewards. Reinforcement learning process model could be represented by a six-tuple <A, S, R, P, γ, D>. In the six-tuple, A represents action space, S is state space, R is reward function R(s, *a*), indicates the immediate reward the Agent is expected to get when executes action *a* in the state *s*. P represents the probability function P (s, a, s'), indicates the possibility that after Agent executed action *a* then reaches state s' in the state s. γ is discount factor, $0 \le \gamma < 1$. D represents the initial state distribution.

Although reinforcement learning can be applied to image segmentation and has good performance, but it still has some limitations, including: when faced with dynamically changing environment, the target itself may change. In this case, if the target itself has changed, the learned strategies would fail. Therefore, it needs to re-learn the optimal policy. When the targets are not only one, i.e. it is not a problem with a single target but multiple targets; it is difficult for most of the reinforcement learning approaches to adapt the situation. If the environment is complicated, and the state space is huge, it would lead to a bad real time of reinforcement learning. Besides, there are some cases, which the state space is too huge to use reinforcement learning algorithms. When addressing the issue of image segmentation, there often exists some uncertain factors, which makes it difficult for algorithm to obtain accurate environment status and feedback information, it may cause that reinforcement learning algorithm cannot converge.

In 2013, Zhao and Tan[9] proposed a multi-motive reinforcement learning approach, adding motive space to former state space to two-layer map structure of action space, so that transforming it into the three-layer map structure which from the state space to action space, then from motives space to action space. It makes the algorithm could take advantage of priori knowledge. In addition, it enhances the flexibility of reinforcement learning algorithms and improves the efficiency of the algorithm.

3 The proposed methodology

3.1 PROBLEM MODELING

According to traditional threshold based image segmentation approach[10], in general, the grey levels of an image is assumed to be 1-m, and the number of the pixels whose grey level is *i* is represented as n_i, then the total number of the pixels of the image is as follows:

$$N = \sum_{i=1}^{m} n_i . \tag{1}$$

The probabilities of each grey level are as follows:

$$P_i = \frac{n_i}{N} . \tag{2}$$

Using variable k to divide them into two groups A_0=[1,…,k], A_1=[k+1,…,m], then the probability of A_0 is:

$$w_0 = \frac{\sum_{i=1}^{k} n_i}{N} = \sum_{i=1}^{k} p_i . \tag{3}$$

The probability of A_1 is:

$$w_1 = \sum_{i=k+1}^{m} p_i = 1 - w_0 . \tag{4}$$

The average value of grey level of A_0 is:

$$u_0 = \frac{\sum_{i=1}^{m} P_i \times i}{w_0} . \tag{5}$$

The average value of grey level of A_1 is:

$$u_1 = \frac{\sum_{i=k+1}^{m} P_i \times i}{w_1} . \tag{6}$$

So the grey level of the whole image is:

$$u = \sum_{i=1}^{m} P_i \times i . \tag{7}$$

The average value of grey scale whose threshold is k is as follows:

$$u(k) = \sum_{i=1}^{k} P_i \times i . \tag{8}$$

The sampled average value is $\mu = w_0 u_0 + w_1 u_1$, the variance is:

$$d(k) = w_0 (u_0 - u)^2 + w_1 (u - u_1)^2 . \tag{9}$$

Therefore, the fitness function can be as follows:

$$d(k) = w_0 w_1 (u_1 - u_2)^2 . \tag{10}$$

The value of variable *k* ranges from 1 to m, and we assumed that the *k** can maximize *d*(*k*), so *k** is the optimal threshold for image segmentation.

This paper utilizes multi-motivate reinforcement learning algorithm to obtain the value of k *. Reinforcement learning for image segmentation trains each set of data. First randomly assigned to the Agent an initial segmentation threshold, dividing original image, Agent calculates the current state, then select an action to change the current segmentation threshold based on the action selective policy. Defining reward (return value) r as the fitting degree of the current segmented target area and the actual optimal image segmentation result; the better the fitting degree of the segmented target area and the actual optimal image segmented, which the obtained threshold makes, the better the obtained threshold, the bigger positive reward Agent gets. Besides, updates matrix of value of Q. Repeat this cycle until matrix of value of Q converges, then end the learning process.

3.2 STATE REPRESENTATION

Every step of the reinforcement learning is that Agent chooses and executes an optimal action for the current state, and so forth, until it reaches the ultimate aim, i.e. the image is segmented successfully. Thus, in the reinforcement learning for image segmentation, the status of Agent is representation of current image. This paper used the approach, which is presented by Zhu et al., using two-tuple {S1, S2} to represent the status of reinforcement learning. S1 is the overlapping ratio of the object contour edge of the segmentation result of current threshold to the edge that is obtained by edge detection. The ratio is higher means the surface segmentation is better. S2 represents the ratio of the target area of current segmentation result to the target area, which is segmented by OSTU. In summary, state S= {S1, S2}.

3.3 MOTIVE AND ACTION REPRESENTATION

The learner changes current segmentation threshold by perform an action. For instance, we defined 14 motives, of which the first 9 motives are m_1 = {- 50, -30, -10, -1, 0, 1, 10, 30, 50}, representing the increment value to current threshold and corresponding to 9 actions. If the current threshold value is k, then after selecting motive m, the corresponding action is adding m to k, i.e., the threshold value is k + m. So the actions according to motive m_1 are a_1 = {k-50, k-30, k-10, k-1, k, k + 1, k + 10, k + 30, k + 50}.

Since we hope that when the current threshold is poor and far from the optimal value, the threshold would be increased significantly. Besides, when the current threshold is close to optimal value, we are willing to change threshold in smaller range near the local optimal solution, and the change should be slightly. So we set the other five motives as m_2 = {double, increase by 50%, increase by 1%, decrease by 1%, decrease by 50%}, if current threshold is k, then these five motives correspond with action a_2 = {2k, 1.5 k, 1.01k, 0.99k, 0.5k}.

In addition, we want to introduce a priori knowledge, so that action selection could be linked directly with the function d(k) that measures the quality of threshold value. Then set two motives as m_3 = {increase d(k), decrease d(k)}, the corresponding actions are making value d(k) increase or decrease of a_1 and a_2.

In summary, motive m = {m_1, m_2, m_3}, action a = {a_1, a_2}. Of course, more appropriate motives and actions can be designed based on the actual application scenarios.

3.4 POLICY FOR MOTIVE AND ACTION SELECTION

According to the MMQ-voting [9] method that Zhao proposed, the main purpose of learning for function Q(s, m) is learning the Q table corresponding to state-action. The selection of action a is not just simply a choice based only motive m, but multi-motive, which combine many motives which might participate in the selection of action together in the state *s*, based on the value of function Q of these motives, weighted voting for each action, then selecting the appropriate action. Setting the voting weights W (Q) makes sure there is a positive relation between the weights of W(Q) and value of Q. During each step of the learning process, select n motives which have the maximum value of Q, then utilize these n motives and their corresponding actions to weighted vote:

$$vote(a) = \sum_{\substack{\text{All the motives } m \text{ that} \\ \text{corresponding to action } a}} e^{Q(s,m)} . \quad (11)$$

We select the action, which has the maximum value of Q, there is a positive relation between each action and its value of function Q. Thus, the algorithm tends to make the value Q to be bigger in the learning process.

In the MMQ-voting method, the optimal policy to learn can be expressed as:

$$\pi^*(s)=\arg \max_a vote(a) . \quad (12)$$

The right side of the equation represents the selected action after the voting. Function Q (s, m) is rewritten as the following equation:

$$Q(s,m)=r(s, \arg \max_a vote(a)) + \gamma V^*(\delta(s, \arg \max_a vote(a))). \quad (13)$$

With updating rules for function Q, when updating the evaluation function Q (s, m), you should update all the value Q of motives that all the actions which take part in the selection are corresponding to. The algorithm can be described as follows:

Algorithm Image Segmentation Based on Multi-Motive Reinforcement Learning and OTSU

Initialization the value of Q (s, m);
Set the initial state;
while not convergence do
begin
Calculate the state value *s*.
According to the current state value *s*, choose *n* motives which have maximum value of Q(s,m);
Calculate the vote value of each action by following equation:

$$vote(a) = \sum_{\substack{\text{All the motives } m \text{ that} \\ \text{corresponding to action } a}} e^{Q(s,m)}$$

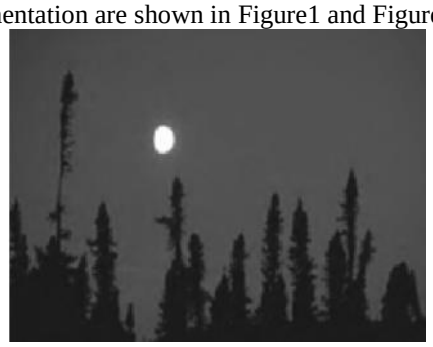
Select the action *a* which has the highest value of vote(a).
Execute action *a*, get a new image segmentation threshold value k;
According to k, generate a new state value s';
Calculate the fitness of the current divided target area and the actual optimal image segmentation result using k and, then obtain reward value *r*;
According to *r*, update value Q(s,m) of every motive m which participates in the vote:

$$Q(s,m)=r(s, \arg \max_a vote(a)) + \gamma V^*(\delta(s, \arg \max_a vote(a)))$$

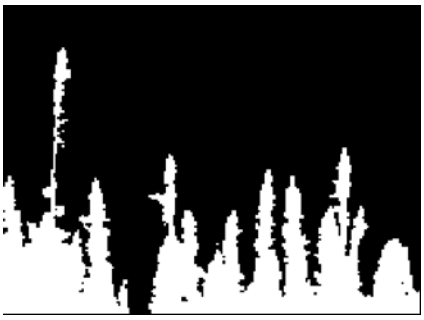
S←S';
end
The current value of *k* is the optimal image segmentation threshold for this kind of images. ▌

4 Experimental results and analysis

Experiments are conducted on Intel(R) Core i5 2.50 GHz CPU with a RAM of 4.00 GB. We select two images as experimental images, use the proposed algorithm compared with traditional reinforcement learning image segmentation algorithm. The images both before and after the segmentation are shown in Figure1 and Figure 2.



(a) Scenery image before segmentation



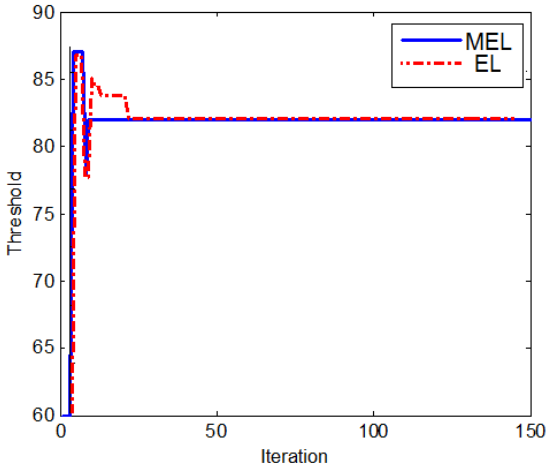
(b) Scenery image after segmentation

FIGURE 1 Segmentation of a scenery image of trees

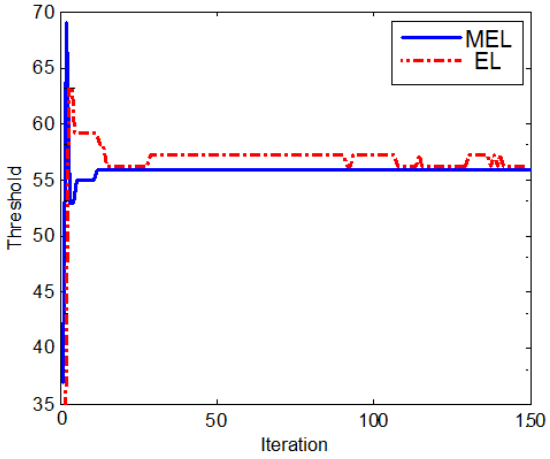
(a) Sky and birds image before segmentation

(b) Sky and birds image after segmentation

FIGURE 2 Segmentation of a sky and birds image



(a) Threshold at each learning iteration for the image1l



(b) Threshold at each learning iteration for the image12

FIGURE 3 Comparison of the learning speed for segmentation, MEL is presented as the proposed Multi-motive

Figure 3 shows comparison about speed of learning segmentation threshold between the proposed approach in this paper and traditional reinforcement learning image segmentation approach. It can be seen that, compared with traditional approaches, the proposed approach can be quicker to learn the optimal threshold. Since the images of the experiment is relatively simple gray-scale image, so the two approaches could both quickly obtain the optimal segmentation threshold, but the proposed algorithm, by introducing multi-motive, makes the learning process more flexible, indirectly related with function d(k), so that the learning process has better and real-time capacity.

5 Conclusions and future works

To improve the efficiency of traditional image segmentation algorithm, in this paper, we present an efficient image segmentation algorithm based on multi-motive reinforcement learning, in OTSU framework, multi-motive reinforcement learning algorithm is adopted to obtain the

optimal segmentation threshold. The state of reinforcement learning is presented as tuple $\{S_1,S_2\}$. S_1 is the overlapping ratio of the object contour edge of the segmentation result of current threshold to the edge that is obtained by edge detection. S_2 represents the ratio of the target area of current segmentation result to the target area, which is segmented by OSTU. The reward is defined as the fitness of the current segmented target area and the actual optimal image segmentation result. The selection of action is based on multiple motives according to the value of Q function of these motives and weighted voting for each action. Compared to traditional approaches, the proposed approach has more flexibility and is facilitate to integrate priori knowledge. The experimental result illustrated the effectiveness of the approach. Future research will be focus on improve the efficiency of the algorithm combined with Bayesian networks based machine learning algorithms [11-15].

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